

ERRATA

Abstract Algebra, Third Edition

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(most recently revised on December 18, 2009)

These are errata for the Third Edition of the book. Errata from previous editions have been fixed in this edition so users of this edition do not need to refer to errata files for the Second Edition (on this web site). Individuals using the Second Edition, however, must make corrections from this list as well as those in the Second Edition errata files (except for corrections to text only needed in the Third Edition; for such text no reference to Second Edition page numbers is given below). Some of these corrections have already been incorporated into recent printings of the Third Edition.

page vi (2nd Edition p. vi)

from: 7.3 Ring Homomorphisms and Quotient Rings

to: 7.3 Ring Homomorphisms and Quotient Rings

page 2, Proposition 1(1) (2nd Edition p. 2, Proposition 1(1))

from: The map f is injective

to: If A is not empty, the map f is injective

page 4, line -3 (2nd Edition p. 5, line 3)

from: $a, b \in \mathbb{Z} - \{0\}$

to: $a, b \in \mathbb{Z}$ and $b \neq 0$

page 31, The group S_3 table

last line missing

add: $\sigma_6(1) = 3, \sigma_6(2) = 1, \sigma_6(3) = 2$ | $(1\ 3\ 2)$

page 33, Exercise 10, line 2 (2nd Edition p. 33, Exercise 10)

from: its least residue mod m when $k + i > m$

to: its least positive residue mod m

page 34, line 1 of Definition (2nd Edition p. 34, line 1 of Definition)

from: two binary operations

to: two commutative binary operations

page 39, Example 2, line -4

from: $ba = ab^{-1}$

to: $ba = a^{-1}b$

page 45, Exercise 22 (2nd Edition p. 46, Exercise 22)

from: is isomorphic to a subgroup (cf. Exercise 26 of Section 1) of S_4

to: is isomorphic to S_4

page 51, line -1 (2nd Edition p. 52, line -1)

from: see Exercise 1 in Section 1.7

to: see Exercise 4(b) in Section 1.7

page 65, line 2 of Exercise 16(c) (2nd Edition p. 66, Exercise 16(c))

from: if and only H

to: if and only if H

page 71, Exercise 5 (2nd Edition p. 72, Exercise 5)

from: there are 16 such elements x

to: there are 8 such elements x

page 84, line 11 of Example 2 (2nd Edition p. 85, line 11 of Example 2)

from: By Proposition 2.6

to: By Theorem 2.7(1)

page 84, line -6 of Example 2 (2nd Edition p. 85, line -6 of Example 2)

from: By Proposition 2.5

to: By Theorem 2.7(3)

page 86, Exercise 14(d) (2nd Edition p. 87, Exercise 14(d))

from: root

to: roots

page 98, Figure 6

add: hatch marks to upper right and lower left lines of the central diamond (to indicate $AB/B \cong A/A \cap B$).

page 103, line 3 of Definition (2nd Edition p. 104, line 3 of Definition)

from: N_{i+1}/N_i a simple group

to: N_{i+1}/N_i is a simple group

page 114, line 3 in proof of Proposition 2 (2nd Edition p. 116, line 3 of proof)

from: $b \in G$

to: $g \in G$

page 128, second line above last display (2nd Edition p. 130, line -3)

from: any element of odd order

to: any nonidentity element of odd order

page 132, Exercise 33, line -1 (2nd Edition p. 134, line -1 of Exercise 33)

from: See Exercises 6 and 7 in Section 1.3

to: See Exercises 16 and 17 in Section 1.3

page 132, Exercise 36(c) (2nd Edition p. 135, Exercise 36(c))

from: g and h lie in the center of G

to: g and h lie in the center of G and $g = h^{-1}$

page 139, Definition (1) (2nd Edition p. 141, Definition (1))

from: A group of order p^α for some $\alpha \geq 1$

to: A group of order p^α for some $\alpha \geq 0$

page 143, last line of first Example (2nd Edition p. 145, line -2)

from: Theorem 17

to: Proposition 17

page 145, line -7 (2nd Edition p. 148, line 5)

from: less than

to: less than

page 148, Exercise 47(i) (2nd Edition p. 151, Exercise 47(i))

from: that has some prime divisor p such that n_p is not forced to be 1

to: for each prime divisor p of n the corresponding n_p is not forced to be 1

page 149, Exercise 54, line 4 (2nd Edition p. 151, line 4 of Exercise 54)

from: G/N acts as automorphisms of N

to: $G/C_G(N)$ acts as automorphisms of N

page 151, Exercise 6, line -2 (2nd Edition p. 153, line -2 of Exercise 6)

from: every pair of elements of D lie in a finite simple subgroup of D

to: every pair of elements of A lie in a finite simple subgroup of A

page 158, line 3 after the Definition (2nd Edition p. 160)

from: n -tuple

to: r -tuple

page 187, Exercise 23, line 4 (2nd Edition p. 189, line 4 of Exercise 23)

from: from G into

to: from K into

page 191, Proposition 2 (2nd Edition p. 193, Proposition 2)

from: nilpotence class at most $a - 1$.

to: nilpotence class at most $a - 1$ for $a \geq 2$ (and class equal to a when $a = 0$ or 1).

page 191, line 3 of the proof of Proposition 2 (2nd Edition p. 193)

from: Thus if $Z_i(P) \neq G$

to: Thus if $Z_i(P) \neq P$

page 194, Theorem 8, line 4 (2nd Edition p. 196, Theorem 8, line 4)

from: $Z_i(G) \leq G^{c-i-1} \leq Z_{i+1}(G)$ for all $i \in \{0, 1, \dots, c-1\}$.

to: $G^{c-i} \leq Z_i(G)$ for all $i \in \{0, 1, \dots, c\}$.

page 198, Exercise 18 (2nd Edition p. 200, Exercise 18)

from: then $G'' = 1$

to: then $G'' = G'''$

page 199, Exercise 22 (2nd Edition p. 201, Exercise 22)

from: Prove that

to: When G is a finite group prove that

page 201, line 2 of Exercise 38 (2nd Edition p. 203, Exercise 38)

from: The group G/M

to: The group P/M

page 209, Proposition 14(1)

from: $n_3 = 7$

to: $n_3 = 28$

page 216, line 4 after displayed steps (1) and (2) (2nd Edition p. 217, line -3)

from: are equal if and only if $n = m$ and $\delta_i = \epsilon_i$, $1 \leq i \leq n$

to: are equal if and only if $n = m$, $r_i = s_i$ and $\delta_i = \epsilon_i$, $1 \leq i \leq n$

page 217, line 2 after first display (2nd Edition p. 218, line 2 after second display)

from: $A(F)$ be the subgroup

to: $A(S)$ be the subgroup

page 260, Exercise 40(iii) (2nd Edition p. 261, Exercise 40(iii))

from: $R/\eta(R)$

to: $R/\mathfrak{N}(R)$

page 263, line 2 of the Definition (2nd Edition p. 264)

from: ring of fractions of D with respect to R

to: ring of fractions of R with respect to D

page 269, line 2 of Exercise 10(c) (2nd Edition p. 270, Exercise 10(c))

from: then A may likewise

to: then P may likewise

page 269, line 2 of Exercise 11(d) (2nd Edition p. 270, Exercise 11(d))

from: Prove that every ideal of

to: Prove that every nonzero ideal of

page 269, lines 1 and 2 of Exercise 11(e) (2nd Edition p. 270, Exercise 11(e))

from: in the direct limit \mathbb{Z}_p satisfying a_j^p

to: in the inverse limit \mathbb{Z}_p satisfying a_j^{p-1}

page 282, second display (2nd Edition p. 283, second display)

$$\text{from: } 0 < N\left(\frac{\alpha}{\beta}s - t\right) = \frac{(ay - 19bx - cq)^2 + 19(ax + by + cz)^2}{c^2} \leq \frac{1}{4} + \frac{19}{c^2}$$

and so (*) is satisfied with this s and t provided $c \geq 5$.

$$\text{to: } 0 < N\left(\frac{\alpha}{\beta}s - t\right) = \frac{(ay - 19bx - cq)^2 + 19(ax + by + cz)^2}{c^2} = \frac{r^2 + 19}{c^2} \leq \frac{1}{4} + \frac{19}{c^2}$$

and so (*) is satisfied with this s and t provided $c \geq 5$ (note $r^2 + 19 \leq 23$ when $c = 5$).

page 283, Exercise 8 (2nd Edition p. 284, Exercise 8)

from: D is a multiplicatively closed subset of R

to: D is a multiplicatively closed subset of R with $0 \notin D$

page 290, line 5 (2nd Edition p. 291, line 5)

from: is irreducible in $\mathbb{Z}[i]$

to: is irreducible in \mathcal{O}

page 304, line 13 (2nd Edition p. 305, line 3)

from: one fewer irreducible factors

to: one fewer irreducible factor

page 306, line 3 (2nd Edition p. 307, line 3)

from: where $p'(x)$ is irreducible in both $R[x]$ and $F[x]$.

to: where $p'(x)$ is irreducible in $R[x]$ if and only if it is irreducible in $F[x]$.

page 312, Exercise 16(b) (2nd Edition p. 313, Exercise 16(b))

from: Prove that f

to: If $f(0) \neq 0$, prove that f

page 318, line 7 after the Definition

from: $L(fg) = L(f) + L(g)$

to: $L(fg) = L(f)L(g)$

page 323, line -6

from: among the differences $S(g_i, g_j)$

to: among the remainders of the differences $S(g_i, g_j)$

page 330, line 7

Replace *from* “We close this section ...” to “Example” with:

We close this section by showing how to compute the basic set-theoretic operations of sums, products and intersections of ideals in polynomial rings. Suppose $I = (f_1, \dots, f_m)$ and $J = (h_1, \dots, h_k)$ are two ideals in $F[x_1, \dots, x_n]$. Then $I + J = (f_1, \dots, f_m, h_1, \dots, h_k)$ and $IJ = (f_1h_1, \dots, f_ih_j, \dots, f_mh_k)$. The following proposition shows how to compute the intersection of any two ideals.

Proposition 30. Suppose $I = (f_1, \dots, f_m)$ and $J = (h_1, \dots, h_k)$ are two ideals in $F[x_1, \dots, x_n]$. If \mathcal{I} denotes the ideal generated by $tf_1, \dots, tf_m, (1-t)h_1, \dots, (1-t)h_k$ in $F[t, x_1, \dots, x_n]$, then $I \cap J = \mathcal{I} \cap F[x_1, \dots, x_n]$. In particular, $I \cap J$ is the first elimination ideal of \mathcal{I} with respect to the ordering $t > x_1 > \dots > x_n$.

Proof: If $f \in I \cap J$, then $f = tf + (1-t)f$, and noting both tf and $(1-t)f$ are in \mathcal{I} shows $I \cap J \subseteq \mathcal{I} \cap F[x_1, \dots, x_n]$. Conversely, suppose $f \in \mathcal{I} \cap F[x_1, \dots, x_n]$. Then $f = a_1tf_1 + \dots + a_mtf_m + b_1(1-t)h_1 + \dots + b_k(1-t)h_k$ for some polynomials $a_1, \dots, a_m, b_1, \dots, b_k$ in $F[t, x_1, \dots, x_n]$. Setting $t = 0$ (which does not alter f) shows f is an $F[x_1, \dots, x_n]$ -linear combination of h_1, \dots, h_k , so $f \in J$. Similarly, setting $t = 1$ shows $f \in I$, so $f \in I \cap J$. Finally, since $I \cap J = \mathcal{I} \cap F[x_1, \dots, x_n]$, $I \cap J$ is the first elimination ideal of \mathcal{I} with respect to the ordering $t > x_1 > \dots > x_n$.

By Propositions 29 and 30, if $I = (f_1, \dots, f_m)$ and $J = (h_1, \dots, h_k)$, then the elements not involving t in a Gröbner basis for the ideal generated by tf_1, \dots, tf_m and $(1-t)h_1, \dots, (1-t)h_k$ in $F[t, x_1, \dots, x_n]$, computed for the lexicographic monomial ordering $t > x_1 > \dots > x_n$, give a Gröbner basis for the ideal $I \cap J$ in $F[x_1, \dots, x_n]$.

page 331, Exercise 3(i)

from: minimum element
to: minimal element

page 332, Exercise 9(b)

from: grlex order
to: grevlex order

page 332, Exercise 15(a)

from: Prove that $\{g_1, \dots, g_m\}$ is a minimal Gröbner basis for the ideal I in R if
to: Prove that the subset $\{g_1, \dots, g_m\}$ of the ideal I in R is a minimal Gröbner basis of I if

page 332, Exercise 16, line 3

from: $(LT(g_1), \dots, LT(g_m), LT(S(g_i, g_j)))$ is strictly larger than the ideal $(LT(g_1), \dots, LT(g_m))$.
 Conclude that the algorithm ...
to: $(LT(g_1), \dots, LT(g_m), LT(r))$ is strictly larger than the ideal $(LT(g_1), \dots, LT(g_m))$, where
 $S(g_i, g_j) \equiv r \pmod{G}$. Deduce that the algorithm ...

page 333, display in Definition following Exercise 33

from: $rJ \in I$
to: $rJ \subseteq I$

page 334, Exercise 43(a)

from: Use Exercise 30
to: Use Exercise 39

page 334, Exercise 43(b)

from: Use Exercise 33(a)
to: Use Exercise 42(a)

page 334, line 3 of Exercise 43(c)

from: ideal defined in Exercise 32,
to: ideal quotient (cf. Exercise 41),

page 348, line 6 (2nd Edition p. 329, line 6)

from: When R is a field, however
to: When R is a field and $M \neq 0$, however

page 350, line 2 of Exercise 4 (2nd Edition p. 331, Exercise 4)

from: $\varphi(\bar{k}) = ka$
to: $\varphi_a(\bar{k}) = ka$

page 357, Exercise 21(i) (2nd Edition p. 338, Exercise 21(i))

replace (i) with: the map from the (external) direct sum $\bigoplus_{i \in I} N_i$ to the submodule of M generated by all the N_i 's by sending a tuple to the sum of its components is an isomorphism (cf. Exercise 20)

page 372, Corollary 16(2), top line of commutative diagram

from: $M \times \cdots \times M_n \xrightarrow{\iota} M \otimes \cdots \otimes M_n$
to: $M_1 \times \cdots \times M_n \xrightarrow{\iota} M_1 \otimes \cdots \otimes M_n$

page 374, line 2 of second Remark (2nd Edition p. 355 line 2)

from: Section 11.6

to: Section 11.5

page 375, line 4 of Exercise 8 (2nd Edition p. 356, Exercise 8)

from: relation $(u, n) \sim (u', n)$ if and only if $u'n = un'$ in N .

to: relation $(u, n) \sim (u', n')$ if and only if $xu'n = xun'$ in N for some $x \in U$.

page 377, Exercise 23 (2nd Edition p. 357, Exercise 23)

from: Proposition 19

to: Proposition 21

page 385, title of subsection following Proposition 26

from: Modules and $\text{Hom}_R(D, -)$

to: Projective Modules and $\text{Hom}_R(D, -)$

page 396, line -2 above Proposition 36 (2nd Edition p. 376)

from: Exercises 18 and 19

to: Exercises 19 and 20

page 398, proof of Theorem 38 (2nd Edition p. 378)

from: Exercises 15 to 17

to: Exercises 15 and 16

page 399, line 8 (2nd Edition p. 379, line 22)

from: The map $1 \otimes \varphi$ is not in general injective

to: The map $1 \otimes \psi$ is not in general injective

page 401, line 2 of Example 1 (2nd Edition p. 381, line 2 of Example 1)

from: $\mathbb{Z}/2\mathbb{Z}$ not a flat module

to: $\mathbb{Z}/2\mathbb{Z}$ is not a flat module

page 403, Exercise 1(d) (2nd Edition p. 383, Exercise 1(d))

from: if β is injective, α and γ are surjective, then γ is injective

to: if β is injective, α and φ are surjective, then γ is injective

page 405, Exercise 15 (2nd Edition p. 385, Exercise 115)

change exercise to:

Let M be a left \mathbb{Z} -module and let R be a ring with 1.

(a) Show that $\text{Hom}_{\mathbb{Z}}(R, M)$ is a left R -module under the action $(r\varphi)(r') = \varphi(r'r)$ (see Exercise 10).

(b) Suppose that $0 \rightarrow A \xrightarrow{\psi} B$ is an exact sequence of R -modules. Prove that if every \mathbb{Z} -module homomorphism f from A to M lifts to a \mathbb{Z} -module homomorphism F from B to M with $f = F \circ \psi$, then every R -module homomorphism f' from A to $\text{Hom}_{\mathbb{Z}}(R, M)$ lifts to an R -module homomorphism F' from B to $\text{Hom}_{\mathbb{Z}}(R, M)$ with $f' = F' \circ \psi$. [Given f' , show that $f(a) = f'(a)(1_R)$ defines a \mathbb{Z} -module homomorphism of A to M . If F is the associated lift of f to B , show that $F'(b)(r) = F(rb)$ defines an R -module homomorphism from B to $\text{Hom}_{\mathbb{Z}}(R, M)$ that lifts f' .]

(c) Prove that if Q is an injective \mathbb{Z} -module then $\text{Hom}_{\mathbb{Z}}(R, Q)$ is an injective R -module.

page 407, last line of Exercise 27(a) (2nd Edition p. 387, Exercise 27(a))

from: where π_1 and π_2 are the natural projections onto

to: where π_1 and π_2 are the restrictions to X of the natural projections from $A \oplus B$ onto

page 423, line 3 of Exercise 9 (2nd Edition p. 403, Exercise 9)

from: If $\varphi|_W$ and $\tilde{\varphi}$ are

to: If $\varphi|_W$ and $\tilde{\varphi}$ are

page 426, line 2 of Exercise 21(b) (2nd Edition p. 406, Exercise 21(b))

from: $6z$

to: $+6z$

page 433, proof of Theorem 19, line 3

from: $= E_v(f) + \alpha E_g(v)$

to: $= E_v(f) + \alpha E_v(g)$

page 435, Exercise 1

change exercise to:

Let V be a vector space over F of dimension $n < \infty$. Prove that the map $\varphi \mapsto \varphi^*$ in Theorem 20 is a vector space isomorphism of $\text{End}(V)$ with $\text{End}(V^*)$, but is not a ring homomorphism when $n > 1$. Exhibit an F -algebra isomorphism from $\text{End}(V)$ to $\text{End}(V^*)$.

page 442, line -8 (2nd Edition p. 422, line -8)

from: $\varphi : M \rightarrow A$ is an R -algebra

to: $\varphi : M \rightarrow A$ is an R -module

page 445, second display in Theorem 34(2) (2nd Edition p. 425, Theorem 34(2))

from: $\iota(m_1, \dots, m_k) = m_1 \otimes \cdots \otimes m_n \bmod \mathcal{C}(M)$

to: $\iota(m_1, \dots, m_k) = m_1 \otimes \cdots \otimes m_k \bmod \mathcal{C}^k(M)$

page 469, line 1 of Exercise 10 (2nd Edition p. 449, Exercise 10)

from: N an R -module

to: N a torsion R -module

page 479, last sentence of second paragraph (2nd Edition p. 459, second paragraph)

from: the degree of the minimal polynomial for A has degree at most n

to: the minimal polynomial for A has degree at most n

page 510, line 1 of text (2nd Edition p. 490, line 1 of text)

from: F is a commutative ring with

to: F is a nonzero commutative ring with

page 516, line 3 or Remark (2nd Edition p. 496, line 3 of Remark)

from: examples indicates

to: examples indicate

page 526, lines 1 and 2 (2nd Edition p. 505, last paragraph lines 1 and 2)

from: the algebraic α is obtained by adjoining the element α to F

to: the algebraic element α is obtained by adjoining α to F

page 555, Exercise 7, bounds for product (2nd Edition p. 535, Exercise 7)

from: $d \mid n$
to: $d \mid m$

page 566, Example 7, first line after second display

from: we see that $\sigma_p^n = 1$
to: we see that $\sigma_p^n = 1$

page 582, Exercise 17 (2nd Edition p. 563, Exercise 17)

from: Let K/F be any finite extension
to: Let K/F be any finite separable extension

page 584, Exercise 24 (2nd Edition p. 564, Exercise 24)

change exercise to:

Prove that the rational solutions $a, b \in \mathbb{Q}$ of Pythagoras' equation $a^2 + b^2 = 1$ are of the form $a = \frac{s^2 - t^2}{s^2 + t^2}$ and $b = \frac{2st}{s^2 + t^2}$ for some $s, t \in \mathbb{Q}$. Deduce that any right triangle with integer sides has sides of lengths $((m^2 - n^2)d, 2mnd, (m^2 + n^2)d)$ for some integers m, n, d . [Note that $a^2 + b^2 = 1$ is equivalent to $N_{\mathbb{Q}(i)/\mathbb{Q}}(a + ib) = 1$, then use Hilbert's Theorem 90 above with $\beta = s + it$.]

page 585, Exercise 29(b) (2nd Edition p. 565, Exercise 29(b))

from: Prove that the element $t =$
to: Prove that the element $s =$

page 585, Exercise 29(c) (2nd Edition p. 565, Exercise 29(c))

from: Prove that $k(t)$
to: Prove that $k(s)$

page 597, line 1 of Example 2

from: $\mathbb{Q}(\zeta_{13})$, For p
to: For p

page 617, Exercises (2nd Edition p. 598, Exercises)

The first 10 exercises, excluding Exercise 3, are over the field \mathbb{Q} .

page 638, Exercise 18 (2nd Edition p. 619, Exercise 18)

from: Let $D \in \mathbb{Z}$ be a squarefree integer
to: Let $D \neq 1$ be a squarefree integer

page 654, Exercise 16 (2nd Edition p. 635, Exercise 16)

from: Prove that F does not contain all quadratic extensions of \mathbb{Q} .
to: Prove that F does contain all quadratic extensions of \mathbb{Q} . [One way is to consider the polynomials $x^3 + 3ax + 2a$ for $a \in \mathbb{Z}^+$.]

page 670, line 2 of Exercise 34 (2nd Edition p. 648, Exercise 34)

from: $\text{Ass}_R(N) \subseteq \text{Ass}_R(M)$
to: $\text{Ass}_R(L) \subseteq \text{Ass}_R(M)$

page 687, Exercise 13 (2nd Edition p. 662, Exercise 13)*change exercise to:*

Let V be a nonempty affine algebraic set. Prove that if $k[V]$ is the direct sum of two nonzero ideals then V is not connected in the Zariski topology. Prove the converse if k is algebraically closed. [Use Theorem 31.] Give a counterexample to the converse when k is not algebraically closed.

page 707, line 2 of Corollary 37(1) (2nd Edition p. 678, Corollary 29(1))*from:* if and only if D contains no zero divisors of R *to:* if and only if D contains no zero divisors or zero**page 713, line 7 of Example 1***from:* $P_2 \cap \mathbb{Q}[y, z] = (y^5 - z^4)$ *to:* $P_2 = P \cap \mathbb{Q}[y, z] = (y^5 - z^4)$ **page 721, line 4 after commutative diagram (2nd Edition p. 688, line 2)***from:* By Proposition 38(1) [2nd Edition: By Proposition 30(1)]*to:* By Proposition 46(1) [2nd Edition: By Proposition 36(1)]**page 728, Exercise 21, line 1***from:* Suppose $\varphi : R \rightarrow S$ is a ring homomorphism*to:* Suppose $\varphi : R \rightarrow S$ is a ring homomorphism with $\varphi(1_R) = 1_S$ **page 754, line 2 of Exercise 8 (2nd Edition p. 720, Exercise 8)***from:* Observe the*to:* Observe that**page 756, line 1 of proof of Proposition 5 (2nd Edition p. 722, proof of Proposition 5)***from:* $\nu(u) + \nu(v) = \nu(uv) = 1$ *to:* $\nu(u) + \nu(v) = \nu(uv) = \nu(1) = 0$ **page 761, line 3 of proof of Proposition 10 (2nd Edition pp. 727)***from:* $g : A \rightarrow F$ by $f(c) =$ *to:* $g : A \rightarrow F$ by $g(c) =$ **page 767, line 5 (2nd Edition pp. 733)***from:* complete*to:* completes**page 774, line 2 of Exercise 12***from:* in R are relatively prime*to:* in R that are relatively prime**page 775, lines 1 to 3 of Exercise 24(d) (2nd Edition pp. 741–2, Exercise 24(d))***from:* $P_3 = (3, 1 + \sqrt{-5}) = (3, 5 - \sqrt{-5}) \dots\dots$ [Check that $\sqrt{-10} = -(5 - \sqrt{-5})\omega/3$.]*to:* $P_3 = (3, 1 - \sqrt{-5}) = (3, 5 + \sqrt{-5}) \dots\dots$ [Check that $\sqrt{-10} = (5 + \sqrt{-5})\omega/3$.]**page 781, bottom row of diagram (17.9) (2nd Edition p. 748, diagram (17.9))***from:* $0 \rightarrow \text{Hom}_R(A, D) \rightarrow$ *to:* $0 \rightarrow \text{Hom}_R(A', D) \rightarrow$

page 793, line 4 of Exercise 11(c) (2nd Edition p. 760, Exercise 11(c))

from: projection maps $I \rightarrow I_i$
to: projection maps $I \rightarrow I/I_i$

page 794, Exercise 17 (2nd Edition p. 761, Exercise 17)

from: for any abelian group A
to: for any abelian group B

page 800, line -7 (2nd Edition p. 766, line -7)

from: $H^n(G, A) \cong \text{Ext}^n(\mathbb{Z}, A)$
to: $H^n(G, A) \cong \text{Ext}_{\mathbb{Z}G}^n(\mathbb{Z}, A)$

page 801, line 4 (2nd Edition p. 767, line 4)

from: 1 if n is odd
to: a if n is odd

page 812, Exercise 18(a) (2nd Edition p. 778, Exercise 18(a))

from: from $\mathbb{Z}/(m/d)\mathbb{Z}$ to $\mathbb{Z}/m\mathbb{Z}$ if n is odd, and from 0 to 0 if n is even, $n \geq 2$,
to: from 0 to 0 if n is odd, and from $\mathbb{Z}/(m/d)\mathbb{Z}$ to $\mathbb{Z}/m\mathbb{Z}$ if n is even, $n \geq 2$,

page 813, line 3 of Exercise 19 (2nd Edition p. 779, Exercise 19)

from: p -primary component of $H^1(G, A)$
to: p -primary component of $H^n(G, A)$

page 815, line 2 of Proposition 30 (2nd Edition p. 781)

from: group homomorphisms from G to H
to: group homomorphisms from G to A

page 816, line -13 (2nd Edition p. 782, line -13)

from: bijection between the elements of
to: bijection between the cyclic subgroups of order dividing n of

page 823, Exercise 9(b) (2nd Edition p. 789, Exercise 9(b))

from: $H^1(A_n, V) = 0$ for all p
to: $|H^1(A_n, V)| = \begin{cases} 3, & \text{if } p = 3 \text{ with } n = 4 \text{ or } 5 \\ 0, & \text{otherwise} \end{cases}$

page 832, lines -10 and -14 (2nd Edition p. 798, lines -6 and -10)

from: L
to: K

page 853, line 4 of Exercise 17 (2nd Edition p. 819, Exercise 17)

from: Your proof ...
to: Your proof that φ has degree 1 should also work for infinite abelian groups when φ has finite degree.

page 869, line -6 (2nd Edition p. 835, line -6)

from: the isotypic components of G
to: the isotypic components of M

page 885, Exercise 8 (2nd Edition p. 851, Exercise 8)

from: This table contains nonreal entries.

to: This table contains irrational entries.

page 893, line 4 (2nd Edition p. 859, line 4)

from: a proper, nontrivial subgroup of G

to: a proper, nontrivial normal subgroup of G

page 897, line 7(2nd Edition p. 863)

Replace *from* “Let $\psi \dots$ ” to end of proof with:

Let \mathcal{C} be the set of nonprincipal irreducible characters of Q . For each $\psi \in \mathcal{C}$ and each $i = 0, 1, \dots, p-1$ define

$$\psi_i(h) = \psi(x^i h x^{-i}) \quad \text{for all } h \in Q.$$

Since ψ_i is a homomorphism from Q into \mathbb{C}^\times it is also an irreducible character of Q . Thus $P = \langle x \rangle$ permutes \mathcal{C} via the (right) action $\psi^{x^i} = \psi_i$ (see Exercise 10).

If $\psi_i = \psi_j$ for some $i > j$ then $\psi(x^i h x^{-i}) = \psi(x^j h x^{-j})$ and so $\psi(h) = \psi(x^{i-j} h x^{j-i})$ for all $h \in Q$. Let $k = i - j$ so that $\psi = \psi_k$. Thus $\ker \psi = \ker \psi_k$ and it follows that x^k normalizes $\ker \psi$. Since $\langle x \rangle = \langle x^k \rangle$ acts irreducibly on Q , $\ker \psi = 1$. Thus ψ is a faithful character. But G is a Frobenius group so $h \neq x^k h x^{-k}$ for every nonidentity $h \in Q$, contrary to $\psi(h) = \psi(x^k h x^{-k})$. This proves $\psi_0, \dots, \psi_{p-1}$ are distinct irreducible characters of Q , i.e., P acts without fixed points on \mathcal{C} .

Next let $\psi \in \mathcal{C}$ and let $\Psi = \text{Ind}_Q^G(\psi)$. We use the orthogonality relations and the preceding results to show that Ψ is irreducible. Since $1, x^{-1}, \dots, x^{-(p-1)}$ are coset representatives for Q in G and, by Corollary 12, Ψ is zero on $G - Q$ we have

$$\begin{aligned} \|\Psi\|^2 &= \frac{1}{|G|} \sum_{h \in Q} \Psi(h) \overline{\Psi(h)} \\ &= \frac{1}{|G|} \sum_{h \in Q} \sum_{i=0}^{p-1} \psi(x^i h x^{-i}) \sum_{j=0}^{p-1} \overline{\psi(x^j h x^{-j})} \\ &= \frac{1}{|G|} \sum_{i,j=0}^{p-1} \sum_{h \in Q} \psi_i(h) \overline{\psi_j(h)} \\ &= \frac{1}{|G|} |Q| \sum_{i,j=0}^{p-1} (\psi_i, \psi_j)_Q = \frac{1}{|G|} |Q| p = 1 \end{aligned}$$

where the second line follows from the definition of the induced character Ψ , and the last line follows because the previous paragraph gives $(\psi_i, \psi_j)_Q = \delta_{ij}$. This proves Ψ is an irreducible character of G .

Finally we show that every irreducible character of G of degree > 1 is induced from some nonprincipal degree 1 character of Q by counting the number of distinct irreducible characters of G obtained this way. By parts (1) and (2) the number of irreducible characters of G (= the number of conjugacy classes) is $p + (q^a - 1)/p$ and the number of degree 1 characters is p . Thus the number of irreducible characters of G of degree > 1 is $(q^a - 1)/p$. Each $\psi \in \mathcal{C}$ induces to an irreducible character of degree p of G . Characters ψ_i, ψ_j in the same orbit of P acting on \mathcal{C} induce to the same character of G (which is zero outside Q

and on Q it is $\sum_{i=0}^{p-1} \psi_i$). One easily computes that characters in different orbits of P on \mathcal{C} induce to orthogonal irreducible characters of G . Since P acts without fixed points on \mathcal{C} , the number of its orbits is $|\mathcal{C}|/p = (q^a - 1)/p$. This accounts for all irreducible characters of G of degree > 1 , and all such have degree p . The proof is complete.

page 899, line 1 of item (3) (2nd Edition p. 865)

from: let Q_3 be a Sylow 11-subgroup of G

to: let Q_3 be a Sylow 13-subgroup of G

page 907, Exercise 1(a) (2nd Edition p. 873, Exercise 1(a))

from: a 3-tuple in $A \times A \times A$ maps to an ordered pair in $A \times A$

to: an ordered pair in $A \times A$ maps to a 3-tuple in $A \times A \times A$

page 912, line 6 (2nd Edition p. 878, line 6)

from: if $A \neq B$ or $C \neq D$

to: if $A \neq C$ or $B \neq D$