

February 2
Section 6.5
Answer Questions

Problem #11

$$\int_{-2}^{-1} e^{2x} dx = \left[\frac{1}{2} e^{2x} \right]_{-2}^{-1} = \frac{1}{2} e^{2(-1)} - \frac{1}{2} e^{2(-2)} = \frac{1}{2} e^{-2} - \frac{1}{2} e^{-4}$$

Know: $\int e^{ax} dx = \frac{1}{a} e^{ax} + C$

Problem #25

average value of $f(x) = 6$ on the interval $[0, 10]$

Answer by inspection: 6

Problem #33

average value of $f(x) = x(x - 1)$ on $[0, 2]$

$$\begin{aligned} \frac{1}{2-0} \int_0^2 x(x-1) dx &= \frac{1}{2} \int_0^2 (x^2 - x) dx = \frac{1}{2} \left[\frac{1}{3} x^3 - \frac{1}{2} x^2 \right]_0^2 \\ &= \frac{1}{2} \left[\frac{1}{3} 2^3 - \frac{1}{2} 2^2 \right] - \frac{1}{2} \left[\frac{1}{3} 0^3 - \frac{1}{2} 0^2 \right] = \frac{1}{2} \left[\frac{8}{3} - 2 \right] - \frac{1}{2} [0] = \frac{1}{2} \left[\frac{2}{3} \right] = \frac{1}{3} \end{aligned}$$